the solar concentrator assembly. Finite element shell models of the concentrator were developed using a two-step nonlinear approach, and results were compared to test data. Reasonable model-to-test agreement was achieved for the torus, and results for the concentrator assembly were comparable to the test for several modes.

Acknowledgments

Larry J. Bradford of CAT Flight Services and Rodney Bradford of United Applied Technologies developed the inflatable concentrator assembly described in this Note. John Lassiter and Robert Engberg of the Structural and Dynamics Test Group at Marshall Space Flight Center provided the modal test data used in the study.

References

¹Stewart, J. F., and Martin, J. A., "Dual Fuel Solar Thermal Stage: Ideal Analysis," *Journal of Spacecraft and Rockets*, Vol. 33, No. 5, 1996, pp. 752–754.

²Lassiter, J., "Shooting Star Experiment Prototype Inflatable Strut/Torus Assembly Modal Survey," NASA Marshall Space Flight Center, Rept. ED73(97-69), Huntsville, AL, June 1997.

³Smalley, K. B., Tinker, M. L., and Fischer, R. T., "Investigation of Nonlinear Pressurization and Modal Restart in MSC/NASTRAN for Modeling Thin Film Inflatable Structures," *Proceedings of the 42nd Structures, Structural Dynamics, and Materials Conference*, AIAA, Reston, VA, 2001, pp. 1701–1708.

⁴Griffith, D. T., "Experimental and Analytical Modal Analyses of an Inflated Thin Film Torus," M.S. Thesis, Dept. of Mechanical Engineering, Univ. of Kentucky, Lexington, KY, 2000.

C. Jenkins Guest Editor

Structural Modeling of a Five-Meter Thin-Film Inflatable Antenna/Concentrator

Kurt B. Smalley* and Michael L. Tinker[†]
NASA Marshall Space Flight Center,
Huntsville, Alabama 35812
and
W. Scott Taylor[‡]
Computer Sciences Corporation,
Huntsville, Alabama 35812

Introduction

NFLATABLE structures have been the subject of renewed interest in recent years for space applications such as communications antennas, solar thermal propulsion, and space solar power. A major advantage of using inflatable structures in space is their extremely light weight. An obvious second advantage is on-orbit deployability and related space savings in the launch configuration. A recent technology demonstrator flight for inflatable structures was the Inflatable Antenna Experiment (IAE) that was deployed on orbit from

Received 18 June 2001; revision received 18 March 2002; accepted for publication 28 May 2002. Copyright © 2002 by the American Institute of Aeronautics and Astronautics, Inc. The U.S. Government has a royalty-free license to exercise all rights under the copyright claimed herein for Governmental purposes. All other rights are reserved by the copyright owner. Copies of this paper may be made for personal or internal use, on condition that the copier pay the \$10.00 per-copy fee to the Copyright Clearance Center, Inc., 222 Rosewood Drive, Danvers, MA 01923; include the code 0022-4650/03 \$10.00 in correspondence with the CCC.

the Space Shuttle Orbiter. Although difficulty was encountered in the inflation/deployment phase, the flight was successful overall and provided valuable experience in the use of such structures.¹

Several papers on static structural analysis of inflated cylinders have been written, describing different techniques such as linear shell theory and nonlinear and variational methods, but very little work had been done in dynamics of inflatable structures until recent years. In 1988 Leonard² indicated that elastic beam bending modes could be utilized in approximating lower-order frequencies of inflatable beams. Main et al. wrote a very significant 1995 paper describing results of modal tests of inflated cantilever beams and the determination of effective material properties.³ Changes in material properties for different pressures were also discussed, and the beam model was used in a more complex structure. The paper demonstrated that conventional finite element analysis packages could be very useful in the analysis of complex inflatable structures. An investigation of the dynamics of polyimide thin-film inflated cylinders is described in Ref. 4, and recent dynamic tests/analyses and potential applications of inflatable solar concentrators are discussed in Refs. 5-7.

The purposes of this Note are to discuss the methodology for dynamically characterizing a large 5-m thin-film inflatable reflector and to discuss the test arrangement and results. Nonlinear finite element modal results are compared to modal test data. The work is significant and of considerable interest to researchers because of 1) the large size of the structure, making it useful for scaling studies, and 2) the application of commercially available finite element software for modeling pressurized thin-film structures.

Description of Inflatable Antenna/Concentrator

In Fig. 1, a prototypecircular5-minflatable antenna/concentrator, or collector, manufactured by SRS Technologies, Inc., is shown. The structure consists of a pressurized lenticular/torus assembly



Fig. 1 Inflatable 5-m antenna/concentrator with tapered composite struts and support stand.

^{*}Aerospace Technologist, Structural Dynamics and Loads Group/ED21. Member AIAA.

[†]Aerospace Technologist, Structural Dynamics and Loads Group/ED21. Associate Fellow AIAA.

[‡]Senior Computer Scientist, Structures and Dynamics Group (603). Member AIAA.

supported by three solid composite struts. The lenticular has a 4.82-m diam, whereas the torus has a 6.40 m outside diameter and 61 cm cross-sectional diameter. This collector can function as a space-basedantenna for communications, surveillance, and radiometry, or as a solar concentrator assembly for solar thermal propulsion systems. The inflatable lenticular and torus elements are constructed of NASA Langley Research Center's CP-1 and DuPont's Kapton® polyimide films, respectively, each of which is 256 μ m thick. Silicon-backed Kapton is the adhesive used for joints in the inflatable structures. A reflective coating on the inner lenticular CP-1 film provides the means of collecting radio waves or solar energy.

The tapered composite struts for the prototype structure were formed by layering of a resin-impregnated fabric and have solid cross sections varying from 20-cm diam at the fixed ends to 10-cm diam at the torus attach points. All three struts extend from the torus at 45 deg and toward a point 2.56 m from the torus/lenticular midplane. Note that for spaceflight configurations, the struts would likely be inflatable/rigidizable with hollow cross sections. Following inflation and deployment in space, the struts would harden upon exposure to sunlight or another rigidizing agent. In the configuration of Fig. 1, the support struts are attached to a composite circular base plate.

Inflatable structures in general are extremely lightweight, and the collector described in this Note is no exception. The thin-film inflatable part of the concentrator (in the deflated condition) has a mass of approximately $3.4\,\mathrm{kg}$, and the total mass including the struts is on the order of $9.1\,\mathrm{kg}$.

Test Configuration and Results

For modal testing, the inflatable structure with supporting struts was mounted on a stand (Fig. 1) by means of the circular base plate described in the preceding section. The stand is a truss structure of composite beams anchored with three large metal plates resting on a concrete floor. The heavy metal plates were required due to the impossibility of bolting the stand directly to the floor.

Because of high flexibility of the polyimide film at any location on the inflated part of the collector, and based on previous experience, it was decided to utilize shaker excitation at a location on one of the struts (Fig. 1). It has been found that excitation applied directly on the inflatable surface, without special shaker adapters or thin-film surface treatments, typically is not successful for modal measurements.

Accelerometers were used on the composite struts and support stand for measuring frequency response. However, to avoid mass loading of the inflatable lenticular and torus elements, a noncontact scanning laser vibrometer was employed. Figure 2 shows the location of the laser vibrometer relative to the test article for one series of measurements.

Modal data were obtained for the test configuration as described in this section at room temperature for inflation pressures of 420 and 4.5 Pa (gauge), in the torus and lenticular, respectively. As described in Ref. 5, modal parameters were successfully identified



Fig. 2 Laser vibrometer configuration for dynamic measurements on inflatable components.

Table 1 Comparison of first five experimental and analytical frequencies

Mode number	NASTRAN nonlinear analytical frequency, Hz	Experimental frequency, Hz	% Error
1	1.45	1.16	-25
2	2.05	2.37	14
3	2.52	3.21	21
4	3.56	4.17	15
5	4.86	5.31	8

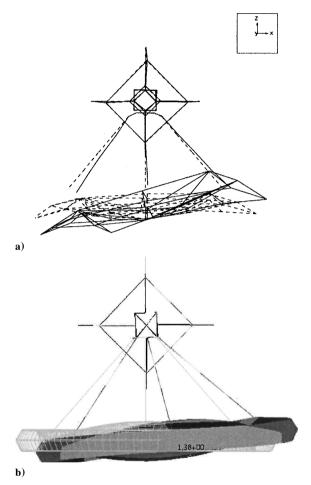


Fig. 3 Fundamental mode shape a) from test and b) for NASTRAN model

for the first five mode shapes of the integrated structure. The first five test frequencies are given in Table 1. The first several mode shapes of the assembly were largely controlled by the composite struts and were relatively insensitive to support stand dynamics. The fundamental experimental mode shape can be seen in Fig. 3 and is clearly characterized by side-to-side flexing of the struts.

Modeling Approach and Results

The finite element modeling technique involved two main steps: 1) nonlinear static analysis, in which the internal pressure loading was applied to the lenticular and torus elements, and 2) modal analysis utilizing the results of step 1. Such a procedure is needed to account for the internal pressure effects on the material stiffness. This two-step modeling and analysis methodology was utilized in the MSC/NASTRAN finite element code and is described in detail in Ref. 7, where results are given for inflatable cylindrical beams.

The lenticular and torus films were modeled using NASTRAN quadrilateral plate elements, each of which was 256 μ m thick. Plate elements of this thickness have extremely low bending stiffness, which approximates membrane behavior, but is believed to help stabilize the nonlinear static solution. Modulus, density, and Poisson's ratio as used were provided by the film manufacturers. The CP-1 film properties are E=2.17 GPa, $\nu=0.34$, and $\rho=1341$ kg/m³,

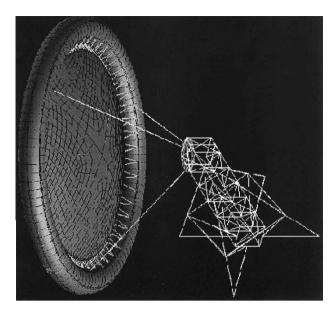


Fig. 4 NASTRAN finite element model of antenna/concentrator assembly.

whereas for Kapton type H film, E = 2.96 GPa, $\nu = 0.34$, and $\rho = 1417$ kg/m³. Internal pressures of 4.5 and 420 Pa (relative or gauge pressures) were applied to lenticular and torus elements, respectively, to account for pressure stiffening of the film. Modeling of the solid-section composite struts and the composite support stand was done using beam elements. Figure 4 shows the finite element model for the antenna assembly.

The mass properties of the inflatable components of the model are very interesting and worthy of discussion. Of a total combined mass of 18.8 kg for the inflatable components, 13.8 kg, or 73%, was attributed to the internal air (air mass calculation based on absolute pressure). Buoyancy force effects suggest the use of relative or gauge pressure in the mass determination. However, modeling experience of the authors for a simple uniform inflated cylinder showed that use of absolute pressure in the computation of internal air mass provided excellent agreement with dynamic test data. Again, however, relative or gauge pressure is used for stiffness modeling.

The greatest difficulty encountered in modeling and analysis was obtaining convergence of the nonlinear static pressurization solution in MSC/NASTRAN. This difficulty is due to the extremely thin polyimide material of which the inflatable components are constructed (256 μm). The ratios of film thickness to overall geometric dimensions such as torus cross-sectional diameter, torus major diameter, and lenticular diameter, appear to be the critical parameters in the nonlinear pressurization analysis.

It was discovered that the model had to be constrained at a large number of points on the film surface to obtain convergence of the pressurizationsolutions. The locations were determined by trial and error. These points were then released in the modal "restart" of NASTRAN, the second step in the analysis procedure. Reference 7 provides an extensive discussion of the convergence issue encountered in these modeling efforts and describes the use of artificial constraints to aid convergence. An alternative approach to stabilizing the nonlinear pressurization computations is recommended by MSC/NASTRAN, in which artificial stiffness terms are added to the model in the early iterations. The extra stiffness terms are removed in later iterations.

A comparison between experimental and model frequency data may be found in Table 1. The first mode of the integrated model occurred at 1.45 Hz (Fig. 3), and the mode shape was characterized by side-to-side flexing of the composite struts with the inflatable components moving rigidly with the struts. This type of behavior was also observed in testing, and the fundamental test and analytical modes compare very well, as seen in Fig. 3.

A finite element model of the 5-m torus with entrained lenticular was modified (with reduced degrees of freedom in the torus-to-lenticular attachments) and reanalyzed in NE/NASTRAN. In this

analysis, the support stand and struts were not included in the model to allow a focus on the critical aspects of the modeling process. However, the torus was restrained at the strut connect points for realism. The pressure load and boundary conditions used previously were retained, and both linear and nonlinear preload modal analyses were performed. The two-run methodology required by MSC/NASTRAN was accomplished more conveniently in NE/NASTRAN in one run. The preload portion of the analysis was accomplished in the first step, and release of the lenticular stabilizing boundary conditions (artificial constraints) was done for step 2. Modal analyses were performed for both linear and nonlinear preloads in step 1.

Comparison of the modal results for the linear and nonlinear preloads showed a pronounced change in the modal response between the two cases. This provided evidence that nonlinear modal solutions are needed for inflatable structures of this type. In both the linear and nonlinear cases, internal pressure was applied to the torus and lenticular, but for the linear analysis, the stiffness matrix was not updated to account for the film deformation.

Conclusions

Modeling of a large 5-m thin-film inflatable collector structure has been accomplished, and comparisons have been made with test data. This work is significant because of 1) the large size of this thin-film structure, 2) the general difficulty in accurately representing the nonlinear material and geometric characteristics of thin-film inflatable structures, and 3) the accomplishment of a modeling methodology that realistically represents the internal pressure loading and the stiffness properties of the thin films in a modal solution.

It was shown that many difficulties were encountered in obtaining convergence of the nonlinear static pressurization procedure in MSC/NASTRAN. In this regard, MSC/NASTRAN was found to have limitations in its nonlinear analysis capability, particularly for large thin-film structures of the type investigated in this Note. NE/NASTRAN appears to be better suited for this analysis (though artificial constraints are still needed), and use of ABAQUS or other finite element packages should also be considered for inflatable structures.

Acknowledgments

SRS Technologies is acknowledged for design and construction of the 5-m structure. Jennie McGee and Jim Moore provided information needed for modeling of the structure and information related to its potential applications. John Lassiter and Robert Engberg of NASA Marshall Space Flight Center's Structures, Mechanics and Thermal Department conducted the dynamic testing and provided the modal test data cited in this Note.

References

¹Freeland, R. E., and Veal, G. R., "Significance of the Inflatable Antenna Experiment Technology," *Proceedings of the 39th Structures, Structural Dynamics, and Materials Conference*, AIAA, Reston, VA, 1998, pp. 2789–2796.

²Leonard, J. W., *Tension Structures: Behavior and Analysis*, McGraw-Hill, New York, 1988, pp. 247, 248.

³Main, J. A., Carlin, R. A., Garcia, E., Peterson, S. W., and Strauss, A. M., "Dynamic Analysis of Space-Based Inflated Beam Structures," *Journal of the Acoustical Society of America*, Vol. 97, No. 2, 1995, pp. 1035–1045.

⁴Slade, K. N., and Tinker, M. L., "Analytical and Experimental Investigation of the Dynamics of Polyimide Inflatable Cylinders," *Proceedings of the 40th Structures, Structural Dynamics, and Materials Conference*, AIAA, Reston, VA, 1999, pp. 2495–2506.

⁵Lassiter, J., and Engberg, R., "5 Meter Inflatable Concentrator Modal Survey Test Report," NASA Marshall Space Flight Center, Rept. SOTV-DEV-00-069, Huntsville, AL, Oct. 2000.

⁶Slade, K. N., Tinker, M. L., Lassiter, J. O., and Engberg, R., "Comparison of Dynamic Characteristics for an Inflatable Solar Concentrator in Atmospheric and Thermal Vacuum Conditions," *Proceedings of the 41st Structures, Structural Dynamics, and Materials Conference*, Vol. 4, AIAA, Reston, VA, 2000, pp. 64–75.

⁷Smalley, K. B., Tinker, M. L., and Fischer, R. T., "Investigation of Nonlinear Pressurization and Modal Restart in MSC/NASTRAN for Modeling Thin Film Inflatable Structures," *Proceedings of the 42nd Structures, Structural Dynamics, and Materials Conference*, AIAA, Reston, VA, 2001, pp. 1701–1708.

C. Jenkins Guest Editor